

# Matchmaking Support for Mathematical Web Services

Simone Ludwig<sup>1</sup>, William Naylor<sup>2</sup>, Julian Padget<sup>2</sup>, Omer Rana<sup>1</sup>

<sup>1</sup>Department of Computer Science, Cardiff University, UK

{scmsal, scmofr}@cs.cardiff.ac.uk

<sup>2</sup>Department of Computer Science, University of Bath, Bath, UK

{wn, jap}@cs.bath.ac.uk

<http://genss.cs.bath.ac.uk>

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Presented by Julian Padget

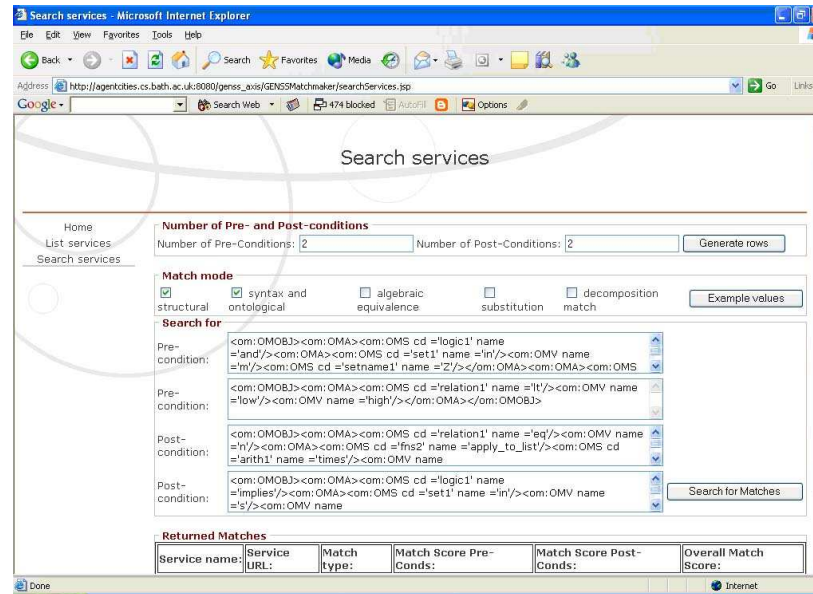
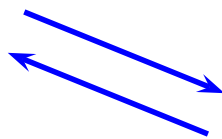
# Outline

- Goals and progress
- Background
- Matchmaking and normalization
- Similarity computation
- Service composition
- Outputs

# The Vision

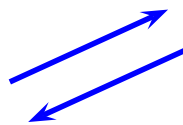
Identification and composition of mathematical web services by functional description:

*e-scientist*



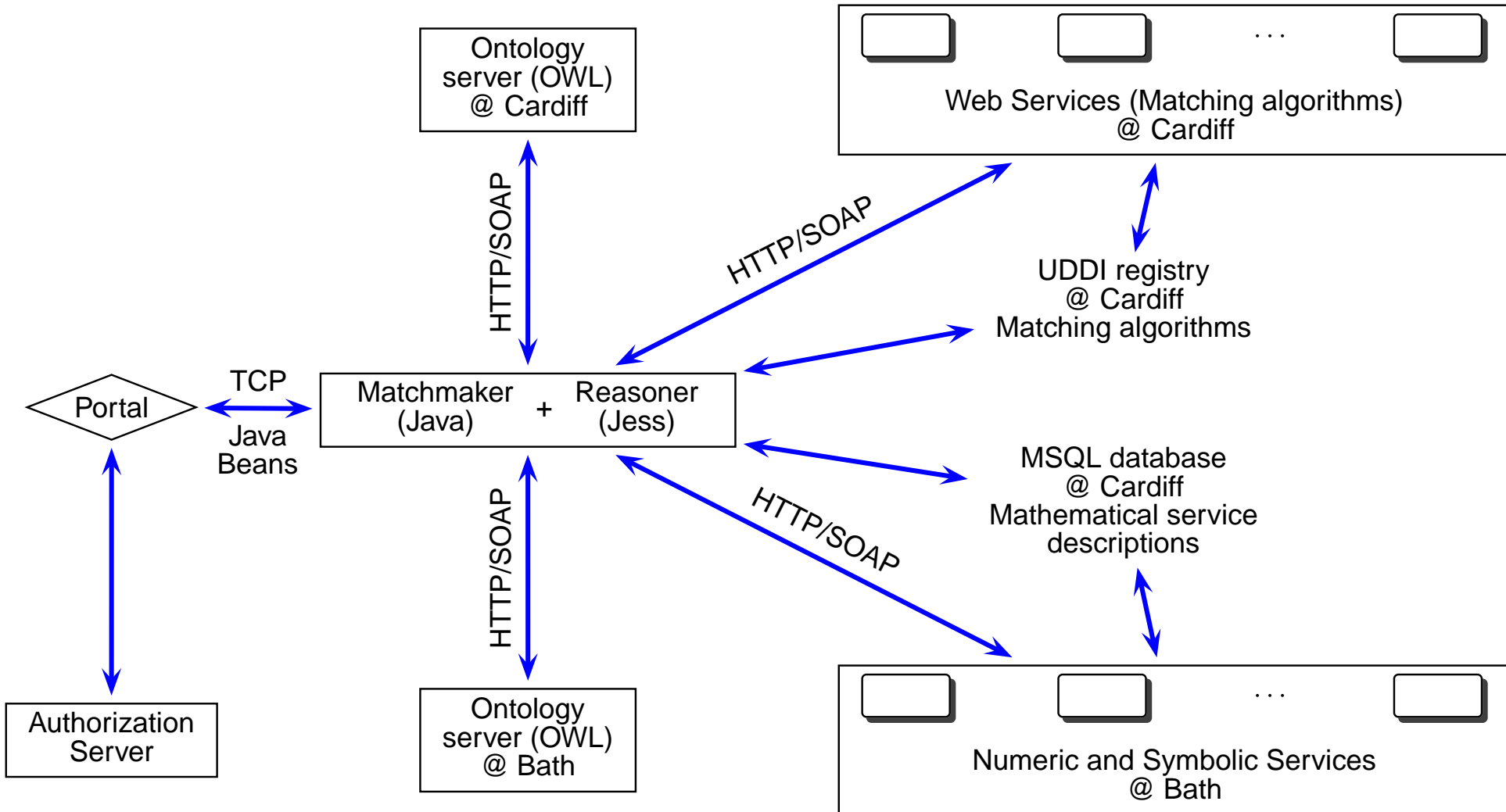
⋮  
*mathematical  
web services*  
⋮

*software  
agent*



Plumbing is easy, saying what you want is not

# The Reality



# From MONET to GENSS



- MONET: <http://monet.nag.co.uk>, EU, 2002–2004
  - ◆ Schema definition: Mathematical Service Description Language, Mathematical Problem Description Language, Mathematical Explanation Language
  - ◆ Basic ontologies: hardware, software, algorithms, problems
  - ◆ OpenMath: <http://www.openmath.org>, mathematical symbols, concepts, organized by content dictionaries (CDs)
  - ◆ Brokerage, service selection by ontological reasoning, orchestration with BPEL4WS
- GENSS: <http://genss.cs.bath.ac.uk>, EPSRC, 2004–2006
  - ◆ Extend matching capability to capabilities and effects
  - ◆ Diversify range of services
  - ◆ Integrate with grid

# GENSS Matchmaking Strategy



Two stages:

- Service registration:
  - 1) Convert service to normal form
  - 2) Put in registryConversion to normal form dominates complexity.
  
- Service lookup:
  - 1) Convert query to normal form
  - 2) Traverse registry, calculating a similarity value between the query and each service
  - 3) Return a list of service URLs ordered on the similarity value.Traversal of the registry dominates complexity.

Matchmaking framework supports plug-ins implemented as web services

# Normalization

- Dissimilar (mathematical) expressions can be equivalent
- No absolute normal form exists
- But can normalize for purpose:
  - ◆ Logical equivalences – standard rewrites
  - ◆ Associative operators – flattened
  - ◆ Context dependent equivalences
  - ◆ Alpha conversions – consistent naming
  - ◆ Commutative operators – reorder arguments
  - ◆ Conversion to disjunctive normal form (cost:  $O(2^n)$ )
- Hence, pre- and post-conditions take the form  $Q(L(R))$ , where:
  - ◆ Q is a quantifier block e.g.  $\forall x \exists y$  s.t.  $\dots$
  - ◆ L is a block of logical connectives e.g.  $\wedge, \vee, \Rightarrow, \dots$
  - ◆ R is a block of relations. e.g.  $=, \leq, \geq, \neq, \dots$

# Matching techniques

- Structural: when task and capability match exactly
- Syntax+Ontology:
  - ◆ Compare elements and attributes in task and capability using taxonomic structure of types to test inclusion
  - ◆ The MONET matcher (to be incorporated)
    - ◇ Sort capabilities that satisfy:  $T_{in} \geq C_{in} \wedge T_{out} \leq C_{out}$
    - ◇ Compute match using DL reasoner
- Function:
  - ◆ Use pre/post-conditions:  $T_{pre} \Rightarrow C_{pre} \wedge C_{post} \Rightarrow T_{post}$ 
    - ◇ *Algebraic equivalence*: show that  $Q - S = 0$  algebraically. In general undecidable, but often works in practice. eg.  $x^2 - y^2$  and  $(x + y)(x - y)$ .
    - ◇ *Value substitution*: show that  $Q - S = 0$  by substituting values into the expression and evaluating. Result is *evidence*, not *proof*.



# Task:capability similarity 1/3

- The similarity measure computation starts from

$$T_{pre} \Rightarrow C_{pre} \wedge C_{post} \Rightarrow T_{post}$$

- Considering the DNF of  $T_{pre}$ ,  $T_{post}$ ,  $C_{pre}$  and  $C_{post}$  as sets of conjuncts, this says:

There exists at least one conjunct in  $C_{pre}$  ( $T_{post}$ ) which is implied by every conjunct in  $T_{pre}$  ( $C_{post}$ )

- More formally the condition is equivalent to:

$$\exists x_1 \in C_{pre} \text{ s.t. } \forall y_1 \in T_{pre} \mid y_1 \Rightarrow x_1$$

and

$$\exists x_2 \in T_{post} \text{ s.t. } \forall y_2 \in C_{post} \mid y_2 \Rightarrow x_2$$

# Task: capability similarity 2/3

- Given two DNF expressions  $R$  and  $S$ :

$$\text{similarity} = \max_{i=1..n} \left\{ \min_{j=1..\tilde{n}} \{M(R_i, S_j)\} \right\}$$

- $M(R_i, S_j)$  calculates a similarity value between two conjuncts (of terms)
- **min** ranges over the *supplier* ( $T_{pre}$  or  $C_{post}$ ) as every conjunct is required, so *min is as good as it gets*
- **max** ranges over the *requirer* ( $C_{pre}$  or  $T_{post}$ ) as any conjunct is possible, so *take the best*

# Task: capability similarity 3/3

- General formula for  $M(R_i, S_j)$

$$M(R_i, S_j) = \sum_{k=1 \dots \delta} m(S_j, R_{i,k}) w_k$$

where  $R_{i,k}$  are the terms in  $R_i$ ,

$w_k$  is a weighting value

and  $m(S_j, R_{i,k})$  is a comparison function – algebraic equivalence or value substitution.

- We weight all terms equally, so take  $w_k = \frac{1}{\delta}$
- $M(S_j, R_{i,k})$  calculates the similarity value of terms and conjuncts.

# Composition of services

- Task:  $T_{pre}, T_{post}$   
Capabilities:  $C_{pre_1}, C_{post_1}$  and  $C_{pre_2}, C_{post_2}$
- Conditions for satisfiability:

$$\begin{aligned} T_{pre} &\Rightarrow C_{pre_1} \\ T_{pre} \wedge C_{post_1} &\Rightarrow C_{pre_2} \\ C_{post_1} \wedge C_{post_2} &\Rightarrow T_{post} \end{aligned}$$

# Current and future work

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- Demonstrate integration with grid services
- Combinatorial Auction and Answer Set solvers as mathematical services
- Release of matchmaker components: plug-ins as web services
- Publication of a repository of mathematical service descriptions
- Demonstration of static and dynamic service composition derived from functional properties of services

[Project ends Spring 2006]